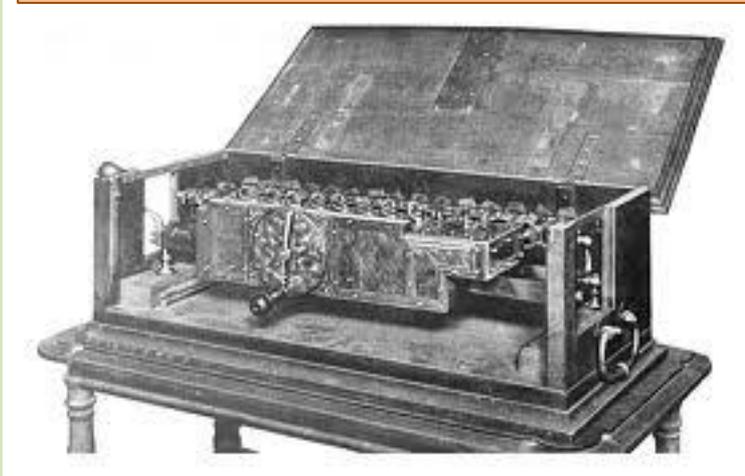




# Gottfried Wilhelm Leibniz

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# The *Stepped Reckoner* of Gottfried Leibniz



He discovered also that computing processes can be done much easier with a binary number coding .

- The great polymath Gottfried Leibniz was one of the first men (after Raymundus Lullus and Athanasius Kircher), who dreamed for a logical (thinking) device.
- Even more—Leibniz tried to combine principles of arithmetic with the principles of logic and imagined the computer as something more of a calculator—as a *logical or thinking machine*.
- In his treatises *De progressionem Dyadica*, March 1679, and *Explication de l'Arithmetique Binaire*, 1703.

# Calculating machine - the binary system

- In the *De progressionem Dyadica* Leibniz even describes a calculating machine which works via the binary system: a machine without wheels or cylinders—just using balls, holes, sticks and canals for the transport of the balls:
- *This [binary] calculus could be implemented by a machine (without wheels)... provided with holes in such a way that they can be opened and closed.*
- *They are to be open at those places that correspond to a 1 and remain closed at those that correspond to a 0.*
- *Through the opened gates small cubes or marbles are to fall into tracks, through the others nothing.*
- *It [the gate array] is to be shifted from column to column as required...!*

# Dream of the general problem-solver

- Leibniz dreamed of inventing the general problem-solver, as well as a universal language:
- *I thought again about my early **plan of a new language or writing-system of reason, which could serve as a communication tool for all different nations...***
- *If we had such an universal tool, we could discuss the problems of the metaphysical or the questions of ethics in the same way as the problems and questions of mathematics or geometry.*
- *That was my aim: **Every misunderstanding should be nothing more than a miscalculation (...), easily corrected by the grammatical laws of that new language.** Thus, in the case of a controversial discussion, two philosophers could sit down at a table and just calculating, like two mathematicians, they could say,  
'Let us check it up ...'*

# Leibniz, the Predecessor of Cybernetics

- Certainly the impressive ideas and projects of Leibniz had to wait some centuries, to be fulfilled.
- The ideas of Leibniz will be used two and half centuries later by **Norbert Wiener**, the founder of Cybernetics.
- So, let's ground and examine his famous *Stepped Reckoner*.

# Similar a pedometer device

- Leibniz got the idea of a calculating machine most probably **in 1670 or 1671**, seeing a pedometer device.
- The breakthrough happened however in 1672, when he moved for several years to Paris, where he got access to the unpublished writings of the two greatest philosophers—**Pascal** and Descartes.
- Most probably in this year he became acquainted (reading Pascal's *Pensees*) with the **calculating machine of Pascal** (Pascaline), which he decided to improve in order to be possible to make not only addition and subtraction, but also multiplication and division.

# Famous stepped-drum machine

- At the beginning, Leibniz tried to use a mechanism, similar to Pascal's, but soon realized, that for multiplication and division it is necessary to create a completely new mechanism, which will make possible **the multiplicand (dividend) to be entered once and then by a repeating action (rotating of a handle) to get the result.**
- Trying to find a proper mechanical resolution of this task Leibniz made several projects, before to invent his famous *stepped-drum mechanism*.
- One of his projects (see the nearby sketch) describes something very similar to the pin-wheel mechanism, which will be reinvented in 1709 by **Giovanni Poleni**.
- The undated sketch is inscribed "*Dens mobile d'une roue de Multiplication*" (the moving teeth of a multiplier wheel).
- Some historians even assume, that the pin-wheel was used in one version of the Leibniz's calculating machine, which didn't survive to the present (the machine was under continuous development more than 40 years and several copies were manufactured).

# First Obstacles – Possibilities of Fine Mechanics

- Starting to create the first prototype, Leibniz soon faced the same obstacles that Pascal had experienced:  
poor workmanship, unable to create the fine mechanics, required for the machine.
- He complained:  
*"If only a craftsman could execute the instrument as I had thought the model."*

# The first wooden prototype

- The first wooden prototype of the *Stepped Reckoner* (this is a later name, actually Leibniz called his machine ***Instrumentum Arithmeticum***) was ready soon and **in the end of 1672** and beginning of 1673 it was **demonstrated to some of his colleagues at French Academy of Sciences**, as well as to the Minister of Finances Jean-Baptiste Colbert.
- Then Leibniz was sent to London with a diplomatic mission, where he succeeded not only to meet some English scientists and to present his treatise called *The Theory of Concrete Motion*, but also **to demonstrate the prototype of his calculating machine to the Royal Society on 1st of February, 1673.**
- The demonstration was probably not very successful, because the inventor admitted that the instrument wasn't good enough and promised to improve it after returning to Paris.
- Nevertheless, the impression of Leibniz must have been very positive, because **he was elected as a member of Royal Society in April, 1673.**

# Arithmetic machine – easy, fast, reliable

- In a letter of 26th of March 1673 to one of his correspondents—Johann Friedrich, mentioning the presentation in London  
Leibniz described the purpose of the *arithmetic machine* as making calculations ***easy, fast, and reliable.***
- Leibniz also added that theoretically the numbers calculated might be as large as desired, if the size of the machine was adjusted: *a number consisting of a series of figures, as long as it may be (in proportion to the size of the machine).*

# First metal prototype

- Back in Paris, Leibniz hired a **skilful mechanic**—the local **clockmaker Olivier**, who was a fine craftsman, and he made the first metal (brass) prototype of the machine.
- It seems the first working properly device was ready as late as in 1685 and didn't manage to survive to the present day, as well as the second device, made 1686-1694.
- **Olivier used to work for Leibniz up to 1694.**
- Later on professor Rudolf Wagner and the mechanic Levin from Helmstedt worked on the machine, and after 1715, the mathematician Gottfried Teuber and the mechanic Haas in Leipzig did the same.

# Appreciation by Arnauld and Huygens

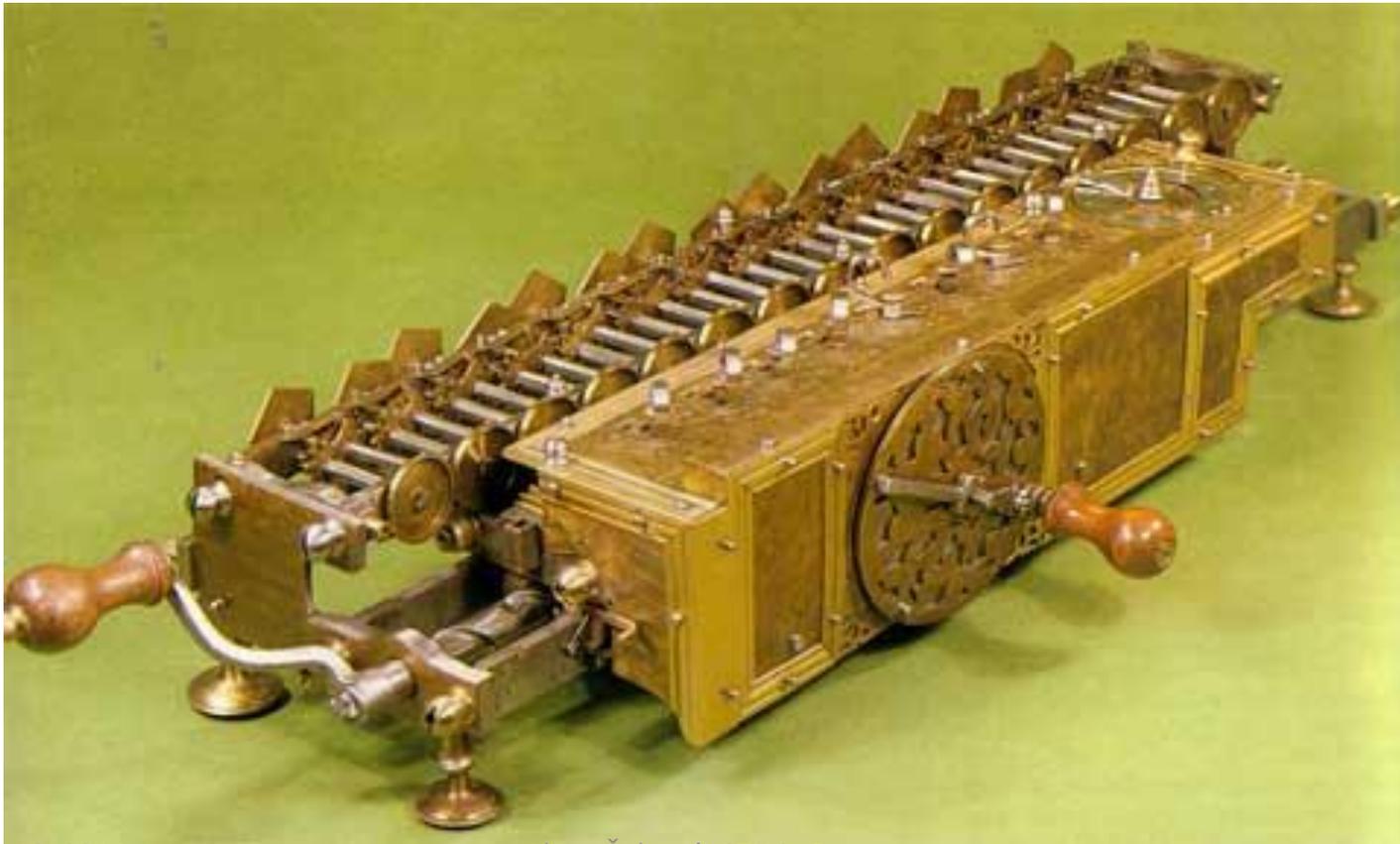
- In 1675 the machine was presented to the French Academy of Sciences and was highly appreciated by the most prominent members of the Academy—**Antoine Arnauld** and **Christian Huygens**.
- Leibniz was so pleased by his invention, that he immediately informed some of his correspondents: e.g. Thomas Burnett, 1st Laird of Kemnay:
- *I managed to build such **arithmetic machine, which is completely different of the machine of Pascal, as it allows multiplication and division of huge numbers to be done momentarily, without using of consecutive adding or subtraction**, and to other correspondent, the philosopher Gabriel Wagner—I managed to finish my arithmetical device. **Nobody had seen such a device, because it is extremely original.***

# Today – two old machines

- **It is unknown how many machines were manufactured by order of Leibniz.**
- It is known however, that the great scientist was interested in this invention all his life.
- **He spent on his machine a very large sum at the time—some 24000 talers according to some historians, so it is supposed the number of the machines to be at least 10.**
- One of the machines (probably third manufactured device), produced 1690-1720, was stored in an attic of a building of the **University of Göttingen** sometime late in the 1770s, where it was completely forgotten. It remained there, unknown, until 1879, when a work crew happened across it in a corner while attempting to fix a leak in the roof.
- **In 1894-1896 Arthur Burkhardt** restored it, and it has been kept at the Niedersächsische Landesbibliothek for some time.
- **At the present time exist two old machines**, which probably are manufactured during Leibniz's lifetime (in the **Hanover State Library** and **in the Deutsches Museum in München**), and several replicas (see one of them in the photo below).

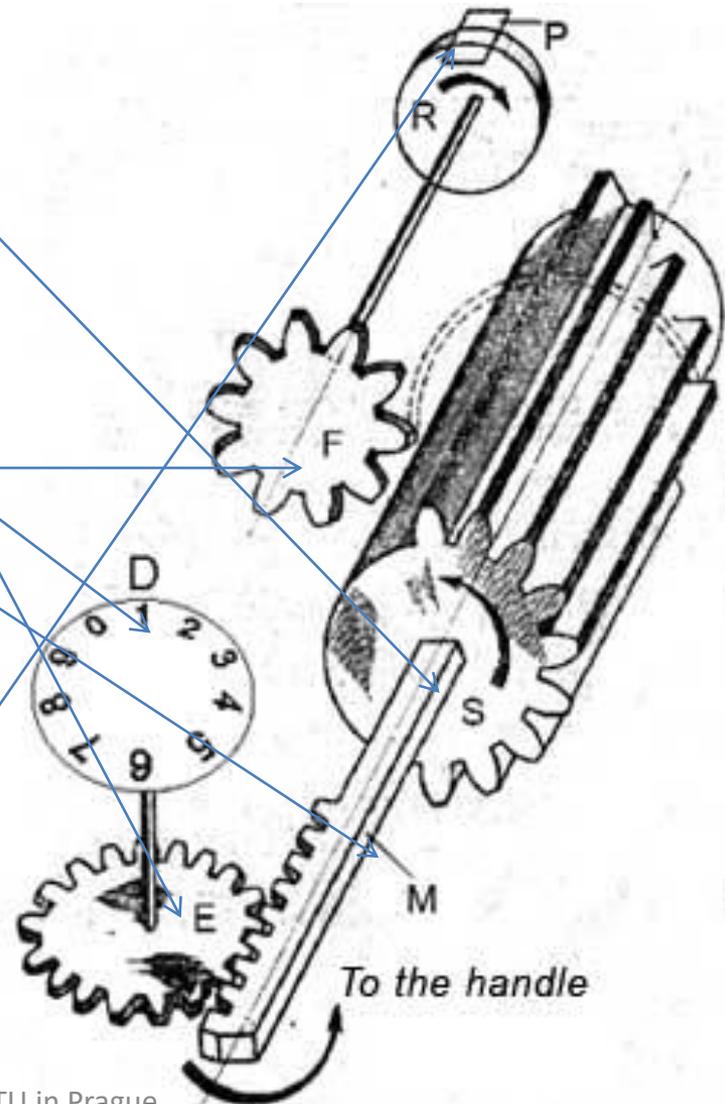
# Replica

The mechanism of the machine is  
67 cm long, 27 cm wide and 17 cm high  
and is housed in a big oak case with dimensions 97/30/25 cm.



# The stepped-drum mechanism

- The stepped-drum (marked with *S* in the sketch) is attached to a four-sided axis (*M*), which is a teeth-strip. This strip can be engaged with a gear-wheel (*E*), linked with the input disk (*D*), on which surface are inscribed digits from 0 to 9.
- When the operator rotates the input wheel and the digits are shown in the openings of the lid, then the stepped drum will be moved parallel with the axis of the 10-teeth wheel (*F*) of the main counter.
- When the drum rotated to a full revolution, with the wheel (*F*) will be engaged different number of teeth, according to the value of the movement, which is defined by the input disk and the wheel (*F*) will be rotated to the appropriate angle.
- Together with the wheel (*F*) will be rotated linked to it digital disk (*R*), whose digits can be seen in the window (*P*) of the lid. During the next revolution of the drum to the counter will be transferred again the same number.

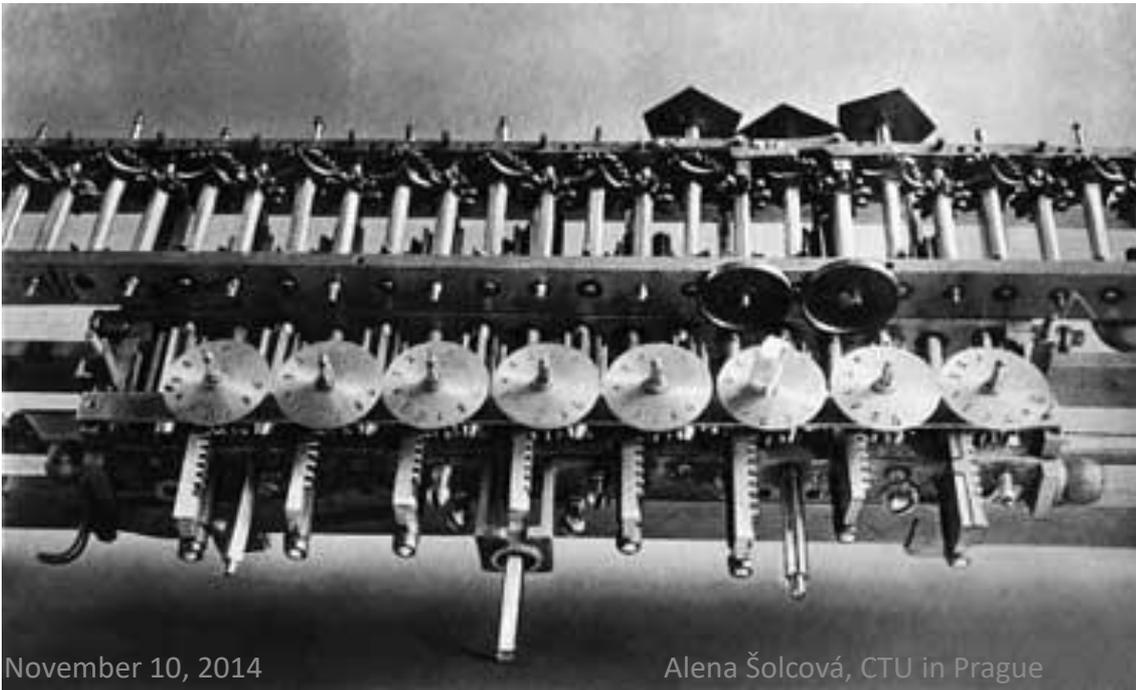


# The Mechanism without Cover

The input mechanism of the machine is **8-positional**, i.e. it has 8 stepped drums, so after the input of the number by means of input wheels, **rotating the front handle** (which is connected to the main wheel (called by Leibniz *Magna Rota*))

All digital drums will make 1 revolution each, adding the digits to the appropriate counters of the digital positions.

**The output (result) mechanism is 12-positional.**



The result (digits inscribed on the digital drums) can be seen in the 12 small windows in the upper unmovable part of the machine.

# The Tens Carry Mechanism

The tens carry mechanism (© Aspray, W., Computing Before Computers)

When a carry must be done, the rod (7) will be engaged with the star-wheel (8) and will rotate the axis in a way, that the bigger star-wheel (11) will rotate the pinion (10).

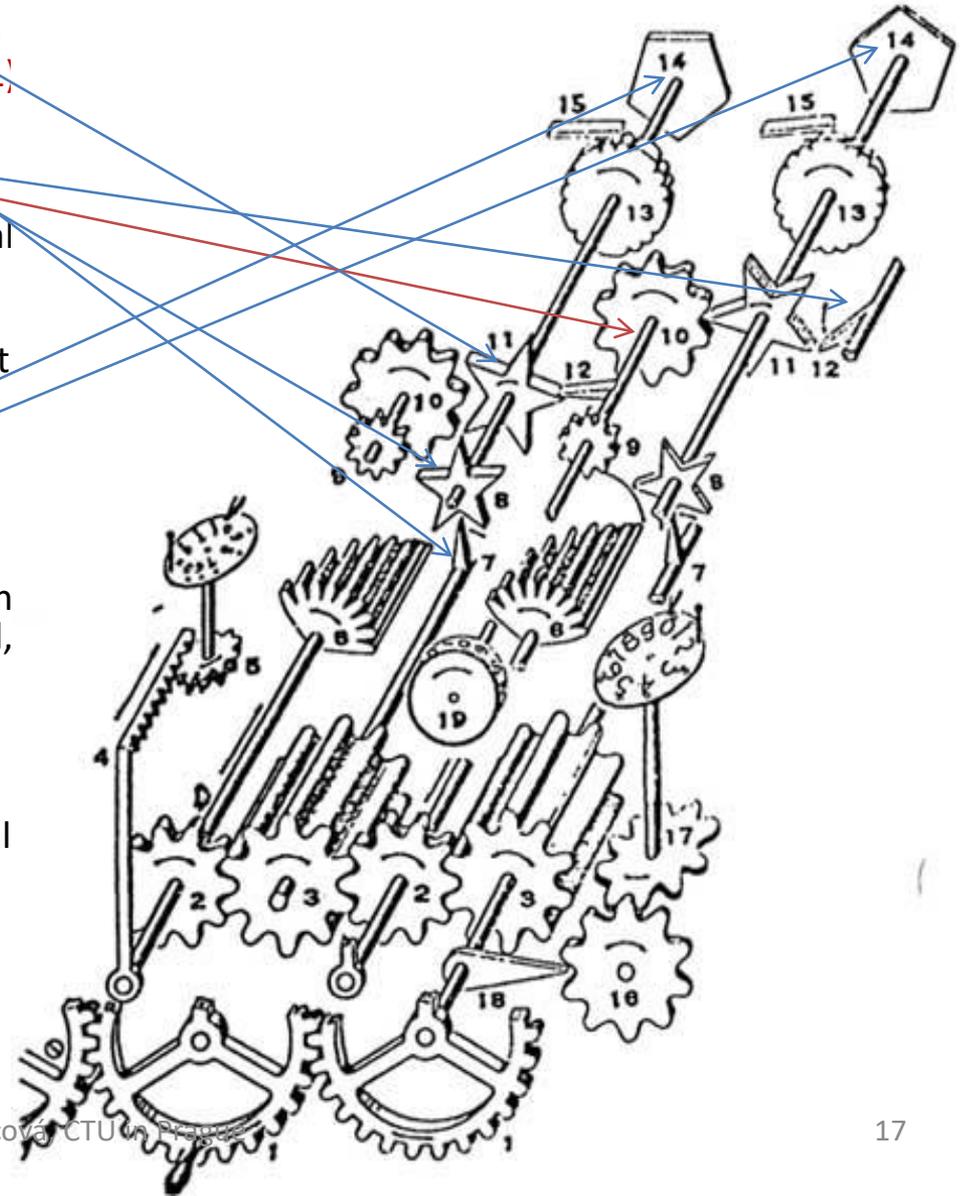
On the axis of this pinion is attached a rod (12), which will be rotated and will transfer the motion to the star-wheel (10) of the next digital position, and will increase his value with 1. So the carry was done.

The transfer of the carry however will be stopped at this point, i.e. if the receiving wheel was at the 9 position, and during the carry it have gone to 0 and another carry must be done, this will not happen.

There is a workaround however, because the pentagonal disks (14) are attached to the axis in such way, that their upper sides are horizontal, when the carry has been done, and with the edge upwards, when the carry has not been done (which is the case with the right disk in the sketch).

If the upper side of the pentagonal disk is horizontal it cannot be seen over the surface of the lid, and cannot be noticed by the operator, so manual carry is not needed.

If however the edge can be seen over the surface of the lid, this will mean that the operator must rotate manually this disk, performing a manual carry.



# An outside sketch

Based on the drawing from *Theatrum arithmetico-geometricum* of Leupold

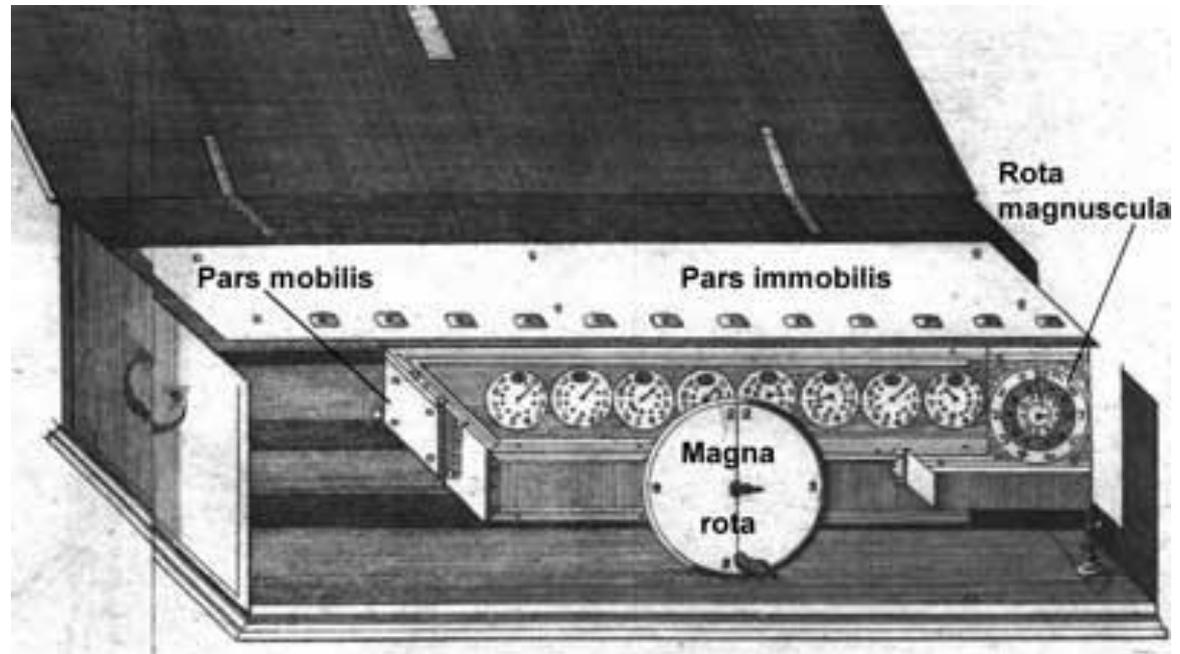
The mechanism of the machine can be divide to 2 parts.

The upper part is unmovable and was called by Leibniz

*Pars immobilis*.

The lower part is movable and is called

*Pars mobilis*.



In the *Pars mobilis* is placed the 8-positional setting mechanism with stepped drums, which can be moved leftwards and rightwards, so to be engaged with different positions of the 12-positional unmovable calculating mechanism.

# Adding, Subtraction, and Other Operation

- **Adding with the machine is simple**
  - first addend is entered directly in the result wheels (windows) (there is a mechanism for zero setting and entering numbers in the result wheels),
  - second addend is entered with the input wheels in the *Pars mobilis*, and then the forward handle (*Magna rota*) is rotated once.
- **Subtraction can be made in a similar way,**
  - but all readings must be taken from the red subtractive digits of the result wheels,  
rather than the normal black additive digits.
- **On multiplication,**
  - the multiplicand is entered by means of the input wheels in the *Pars mobilis*,
  - then *Magna Rota* must be rotated to so many revolutions, which number depends on the appropriate digit of the multiplier.
  - If the multiplier is multidigital, then *Pars mobilis* must shifted leftwards with the aid of a crank and this action to be repeated, until all digits of the multiplier will be entered.
- **Division is done by setting the dividend in the result windows** and the divisor on the setup dials, then a turn of *Magna rota* is performed and **the quotient may be read from the central plate of the large dial.**

# To multiply 358

- There is also a counter for number of revolutions, placed in the lower part of the machine, which is necessary on multiplication and division—the large dial to the right of the small setting dials.
- This large dial consists of two wide rings and a central plate—the central plate and outer ring arc inscribed with digits, while the inner ring is colored black and perforated with ten holes.
- If for example we want to multiply a number on the setting mechanism to 358, a pin is inserted into hole 8 of the black ring and the crank is turned, this turns the black ring, until the pin strikes against a fixed stop between 0 and 9 positions.
- The result of the multiplication by 8 may then be seen in the windows. The next step requires that the setting mechanism to be shifted by one place by means of the crank (marked with  $K$  in the upper figure), the pin inserted into hole 5, and the crank turned, where upon the multiplication by 58 is completed and may be read from the windows.
- Again the setting mechanism must be shifted by one place, the multiplication by 3 is carried out in the same manner, and now the result of the multiplication by 358 appears in the windows.

# Better than Pascal

- Leibniz did manage to create a machine, much better than the machine of Pascal.
- The *Stepped Reckoner* was not only suitable for multiplication and division, but also much easier to operate.
- In 1675 during the demonstration of the machine to the French Academy of Sciences, one of the scientists noticed that  
*"...using the machine of Leibniz even a boy can perform the most complicate calculations!"*

# First description

The first description of Leibniz's stepped-drum calculator appeared in **1710**, made by Leibniz himself, in *Miscellanea Berolinensia*, the journal of the Berlin Academy of Sciences.

It was a 3-pages short description, entitled "*Brevis descriptio Machinae Arithmeticae, cum Figura*", and the internal mechanism of the machine is not described.

Habentur & alia Machinamenta superincesso carentia minus vulgò nota, magis tamen operibus ob firmitatem apta & cum successu adhibita, ubi nec dentium, nec trochlearum incesso motus transferitur, & tamen rota rotam etiam in distantis circumagat, & rectilincus circularum, circularis rectilincum efficere potest. Sed talia hoc loco describere, prolixum foret, ubi fundamenta tradere propositum fuit, Frictionis remedia derivantur.

XXXI.

G. G. L.

## Brevis descriptio Machinae

Arithmeticae, cum Figura; quam vid. Fig. 73.

**S**pecimen Machinae Arithmeticae, à me adolescente inventae, quam exhibeo, jam Anno 1673. societati Regiae Londinensi ostendi. Paulo proveciorem mox vidit Academia Regia Parisina. Et tunc quidem Dn. Matthion Mathematicus eruditus Lutetiae agens in edita à se Tabula aeri incisa, qua Orgyiam (Toise) in 1000. partes aequales dividebat, eique operationes in usum vulgarem accommodabat: notavit, machina mea adhibita (quam viderat) calculos à puerulo peragi posse. Mentionem quoque ejus fecit celeberrimus Tschirnhusius in Medicinae Mentis editione novissima. Viri excellentes Antonius Arnauldus, Christianus Hugenius & Melchisedecus Thevenotius, qui viderant, testati sunt per literas quanti facerent, hortatique, ne oblivioni mandaretur.

Consistit ex duabus partibus, *Immobili* & *Mobili*. In parte immobili per foramina duodecim apparent rotulae & in iis notae numericae 000000111085. In parte mobili visitur *Rota una majuscula* & octo minusculae. In Majuscula exterius interiusque inscriptae sunt notae 0. 1. 2 3 4. 5. 6. 7. 8. 9, interque utrumque notarum Circulum est limbus mobilis foraminum decem, notis respondentium. *Rotarum Minuscularum* cuiusvis inscriptae sunt eadem notae, adestque ind. x, qui circumagi potest, & ab his indicibus non trantur notae 00001709, eoque fit, ut eadem notae etiam per eam ind. m rotarum foramina sepe uno aspectu unaque in linea oculo offe. 27

Operatio hæc est: Sit datus numerus Multiplicandus per datum Numerum Multiplicantem, modo Productum non excedat duodecim notas, Ex. gr. 1709. numerus anni currentis multiplicari debeat per 365. numerum dierum; itaque, posito prius per foramina octo rotarum apparuisse non nisi 0, indiculi in rotis quatuor minusculis dextrerrimis admoveantur notis 1709: partis autem mobilis (à situ, qui in figura apparet dextrorsum promotæ) hic sit initio situs: ut nota prima octo Rotarum partis mobilis respondeat notæ primæ duodecim rotarum partis immobilis; uti nunc in figura respondet tertiæ. Porro notæ partis immobilis initio sint itidem non nisi 0. Quia jam 1709. debet multiplicari per 365, multiplicetur primum per 5, quod ita fiet: brevis stylus infigatur foramini, quod respondet Numero 5, in rota majuscula exteriori notato. Deinde *Magna Rota* ( nondum hæcenus memorata ) in medio ferè partis mobilis conspicua, arrepto dextra capulo ejus circumagatur; quo factò simul movebitur limbus mobilis rotæ majusculæ. Is motus continuetur, donec, (quod mox fiet) stylus foramini limbi infixus, & cum limbo circumactus in obstaculum incurrat, quod in Rota Majuscula comparet inter 0. & 9. Quo factò ex resistentia admonebimur, absolutam esse hanc operationem, & per foramina partis immobilis exteriora apparebit productum ex 1709 per 5, nempe 8545. Sed quia plures sunt notæ in multiplicante, & proxima à prima est 6; promovebimus partem mobilem sinistrorsum, ita ut prima nota Rotarum octo, respondeat, secundæ notæ Rotarum duodecim. Hoc factò stylum infixum hæcenus foramini exteriori notato, 5, infigemus foramini etiam exteriori notato, 6, jamque iterum capulo arrepto rotam illam Magnam in Medio partis mobilis positam circumagemus, donec stylus in obstaculum impingat: eaque ratione non tantum numerus multiplicandus 1709 multiplicatus erit per 6, sed etiam productum erit additum producto priori, & notæ partis immobilis dexteriores per foramina comparentes erunt 111085. Superest in multiplicatore nota 3. Itaque iterum uno gradu promoveatur pars mobilis sinistrorsum & stylus infigatur foramini in limbo, quod respondet notæ exteriori 3, atque ita Machina in eo erit statà, quem *Figura* exhibet. Ac tunc demum, circumacta tertium Rota magna, donec obstaculum sentiat, numerus multiplicandus 1709 non tantum multiplicatus erit per 3, sed etiam productum si-

# 2nd Page

$$\begin{array}{r}
 1709 \cdot 365 = \\
 \phantom{1709 \cdot 365 =} 8545 \\
 \phantom{1709 \cdot 365 =} 10254 \\
 \phantom{1709 \cdot 365 =} \underline{5127} \\
 623785
 \end{array}$$

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mul prioribus erit additum, prod:bitque productum integrum ex 1709 multiplicato per 365, nempe 623785.

$$\begin{array}{r} 1709 \\ \underline{365} \\ 8545 \\ \underline{10254} \\ 111085 \\ \underline{5127} \\ 623785 \end{array}$$

Id maximi commodi habet hæc operatio, in *Multiplicatione* vel *Divisione*, quod nihil refert, quantus sit numerus multiplicandus, modo machinæ magnitudinem (hoc loco octo notas) non excedat; eodem enim tempore res peragitur, five multarum five paucarum sit notarum. Mentis nullam fere attentionem requiri manifestum est, ut hoc, quicquid est, merito dici possit, *opus infantum*. *Divisio* eadem facilitate reciproco opere peragitur, nec quæritur nota quotientis, sed ipsa se offert. *Dividendus* collocatur in rotis partis immobilis, ubi dumtaxat & *Residuum* conspicuus manet. *Divisor* exhibetur in rotis minusculis partis mobilis, *Quotiens* per notas singulas circuli interioris, quarum ex aduerso stylus post operationem quiescit, designatur; cum multiplicatio circulo exteriori sit usa pars mobilis in machinæ, durante divisione, quoties opus promovetur dextrorsum; cum in multiplicatione promotum fuerit sinistrorsum. *Additio* concipi potest ut multiplicatio per unitatem, *Subtractio*, ut divisio, cujus quotiens unitas. Ita quatuor, quas vocant, species habemus, quibus omnia alia peraguntur. Quanquam *Additio* & *Subtractio* etiam sine *Multiplicationis* aut *Divisionis* imitatione: perfacile in Machina per se efficiantur, & ita quidem, ut parte mobili opus non sit.